

WIN – week 1 day 2 – Order of operations mini lesson

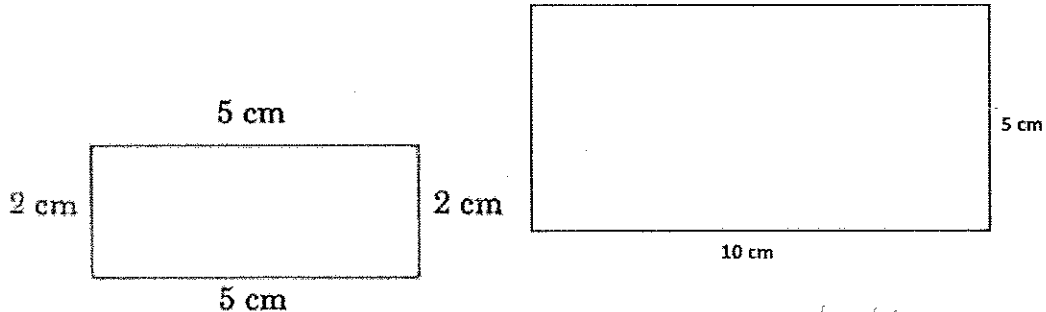
Learning Target: Students will evaluate expressions using the order of operations.

To evaluate an expression means to find its value.

1. Evaluate $4 \cdot 3 + 2 \cdot 5$. $12 + 10 = 22$

Class discussion. Who got 70? Who got 22?

2. I need to find the total Area of the two rectangles below. What process should I follow?



Find each area then add them.

$$= 2 \times 5 + 10 \times 5$$

$$= 10 + 50$$

$$= 60 \text{ cm}^2$$

When we evaluate expressions we follow the order of operations – PEMDAS

P – Parenthesis – evaluate operations inside of grouping symbols first

E – Exponents – Evaluate all the powers

MD – Multiply and Divide from left to right

AS – Add and Subtract from left to right

Practice #15-35 odd

15. 7^2 49

18. $35 - 3 \cdot 8$ 11

21. $24 \div 6 + 2^3 \cdot 4$ 36

24. $(12 - 6) \cdot 5^2$ 150

27. $[(6^3 - 9) \div 23]4$ 36

16. 14^3 2744

19. $-18 \div 9 + 2 \cdot 6$ 14

22. $(11 \cdot 7) - 9 \cdot 8$ 5

25. $3^5 - (1 + 10^2)$ 142

28. $\frac{8 + 3^3}{12 - 7}$ 7

17. 2^6 64

20. $10 + 8^3 \div 16$ 42

23. $29 - 3(9 - 4)$ 14

26. $108 \div [3(9 + 3^2)]$ 2

29. $\frac{(1 + 6)^9}{5^2 - 4}$ 3

Evaluate each expression if $g = 2$, $r = 3$, and $t = 11$.

30. $g + 6r$ 68

31. $7 - gr$ 1

32. $r^2 + (g^3 - 8)^5$ 9

33. $(2r + 3g) \div 4$ 7

34. $t^2 \div 8rt + r^2$ 394

35. $3g(g + r)^2 - 1$ 149

WIN Week 1 Day 3 Multistep equations

Learning target: Students will solve multistep algebraic equations

Equations that require more than one step to solve are called **multistep equations**. To solve such an equation we must use an inverse to undo each step by working backward.

Examples:

Solve each.

$$1. \quad 11x - 4 = 29$$

$$\begin{array}{r} 11x - 4 = 29 \\ +4 \quad +4 \\ \hline 11x = 33 \\ \div 11 \quad \div 11 \\ \hline x = 3 \end{array}$$

$$2. \quad \frac{a+7}{8} = 5 + 8$$

$$\begin{array}{r} a+7 = 110 \\ -7 \quad -7 \\ \hline a = 103 \end{array}$$

3. How is the process of solving #1 different from solving #2?

B/c the entire expression is being divided by 8, you need to undo the division 1st in #2. But in #1 only the 20 is being multiplied by 11 so you need to add the 4 to undo the subtraction 1st.

You try.

$$4. \quad 2a - 6 = 4$$

$$\begin{array}{r} 2a - 6 = 4 \\ +6 \quad +6 \\ \hline 2a = 10 \\ \div 2 \quad \div 2 \\ \hline a = 5 \end{array}$$

$$5. \quad \frac{n+1}{-2} = 15 + 2$$

$$\begin{array}{r} n+1 = -30 \\ -1 \quad -1 \\ \hline n = -31 \end{array}$$

5. Alice is buying a pair of water skis that are on sale for $\frac{2}{3}$ of the original price. After he uses a \$25 gift card, the total cost before taxes is \$115. What was the original price of the skis? Write and solve an equation to help you solve the problem.

$$\begin{array}{l} x = \text{original price} \\ \frac{2}{3}x - 25 = 115 \\ \frac{2}{3}x = 140 \\ \frac{2}{3} \cdot \frac{3}{2} \cdot \frac{2}{3}x = 140 \cdot \frac{3}{2} \\ x = \$210 \end{array}$$

Consecutive integers are integers in counting order such as 4, 5, and 6. You can use the algebraic expressions n , $n+1$, and $n+2$ to represent them. How could you produce consecutive even integers?

6. Find 3 consecutive integers with a ^{add} sum of 21.

$x = 1st \#$
 $x+1 = 2nd \#$
 $x+2 = 3rd \#$

$$x + x + 1 + x + 2 = 21$$

$$3x + 3 = 21$$

$$\begin{array}{r} -3 \quad -3 \\ 3x = 18 \end{array}$$

$$x = 6$$

$$x = 6$$

So 6, 7 & 8
 are the #'s

7. Find three consecutive integers with a sum of -51.

$$x + x + 1 + x + 2 = -51$$

$$3x + 3 = -51$$

$$\begin{array}{r} -3 \quad -3 \\ 3x = -54 \end{array}$$

$$3x = -54$$

$$x = -18$$

So -18, -17 & -16

Practice:

Solve each equation.

1) $6 = \frac{a}{4} + 2$

$$a = 16$$

2) $-6 + \frac{x}{4} = -5$

$$x = 4$$

3) $9x - 7 = -7$

$$x = 0$$

4) $0 = 4 + \frac{n}{5}$

$$n = -20$$

5) $-4 = \frac{r}{20} - 5$

$$r = 20$$

6) $-1 = \frac{5+x}{6}$

$$x = -11$$

7) $\frac{v+9}{3} = 8$

$$v = 15$$

8) $2(n+5) = -2$

$$n = -6$$

9) $-9x + 1 = -80$

$$x = 9$$

10) $-6 = \frac{n}{2} - 10$

$$n = 8$$

11) $-2 = 2 + \frac{v}{4}$

$$v = -16$$

12) $144 = -12(x+5)$

$$x = -7$$

13. Find three consecutive integers with a sum of 54.

$$17, 18, 19$$

WIN Week 1 Day 3 Solving equations with variables on both sides

Learning Target; Students will solve equations with the variable on both sides and equations involving grouping symbols.

To solve an equation with variables on both sides of the equal sign, use the Addition or Subtraction Property of equality to write an equivalent equation with the variable terms on one side. Then isolate the variable.

Example

1. Solve $2+5k=3k-6$. Be sure to check your answer/

$$\begin{array}{r} -3k \quad -3k \\ 2+2k = -6 \\ \hline 2k = -8 \\ k = -4 \end{array}$$

You try:

2. $5a + 2 = 6 - 7a$

$$\begin{array}{r} +7a \quad +7a \\ 12a + 2 = 6 \\ \hline 12a = 4 \\ \hline a = \frac{1}{3} \end{array}$$

3. $3w + 2 = 7w$

$$\begin{array}{r} -3w \quad -3w \\ 2 = 4w \\ \hline \frac{2}{4} = \frac{4w}{4} \\ \frac{1}{2} = w \end{array}$$

4. $8 + 5c = 7c - 2$

$$\begin{array}{r} -5c \quad -5c \\ 8 = 2c - 2 \\ \hline 10 = 2c \\ \hline \frac{10}{2} = \frac{2c}{2} \\ 5 = c \end{array}$$

$$5. \frac{x}{2} + 1 = \frac{1}{4}x - 6$$

$$\begin{array}{r} 2x + 4 = x - 24 \\ \hline x + 4 = -24 \\ \hline x = -28 \end{array}$$

If equations contain grouping symbols (such as parenthesis or brackets) use the distributive property to remove the grouping symbols then solve.

Example

$$\text{Solve } 6(5m - 3) = \frac{1}{3}(24m + 12)$$

$$\begin{array}{r} 30m - 18 = 8m + 4 \\ -8m \quad -8m \\ \hline 22m - 18 = 4 \\ +18 \quad +18 \\ \hline 22m = 22 \end{array}$$

$$\begin{array}{r} 22m = 22 \\ \hline 22 \quad 22 \\ \hline m = 1 \end{array}$$

You try: Solve each of the following

$$6. 8s - 10 = 3(6 - 2s)$$

$$\begin{array}{r} 8s - 10 = 18 - 6s \\ +10s \quad +10s \\ \hline 14s - 10 = 18 \end{array}$$

$$\begin{array}{r} 14s - 10 = 18 \\ +10 \quad +10 \\ \hline 14s = 28 \\ \hline s = 2 \end{array}$$

$$7. 7(n - 1) = -2(3 + n)$$

$$\begin{array}{r} 7n - 7 = -6 - 2n \\ +2n \quad +2n \\ \hline 9n - 7 = -6 \end{array}$$

$$\begin{array}{r} 9n - 7 = -6 \\ +7 \quad +7 \\ \hline 9n = 1 \\ \hline n = \frac{1}{9} \end{array}$$

The equations we have solved so far all have one solution, or one number that when substituted for the variable, makes the equation true. These equations are **SOMETIMES** true. Attempting to solve the equations will result in a single value.

Some equations have no solution. That is, there is no value of the variable that will make the equation true. So these equations are **NEVER** true. Attempting to solve the equation will result in a **FALSE** statement.

Some equations are true for all values of the variable. These equations have infinitely many solutions and are **ALWAYS** true. These equations are called identities. Attempting to solve the equation will result in a true statement.

Number of solutions	When the equation is true	What it looks like Example	Represent the solution
1	Sometimes	$x=7$	$x=7$
0	Never	$5=-14$	No solution
Infinitely many	Always	$5=5$	Infinitely many solutions OR All real numbers

8. Solve

a. $5x + 5 = 3(5x - 4) - 10x$

$$5x + 5 = 15x - 12 - 10x$$

$$5x + 5 = 5x - 12$$

$$-5x \quad -5x$$

$$5 = -12$$

 \emptyset

b. $3(2b - 1) - 7 = 6b - 10$

$$6b - 3 - 7 = 6b - 10$$

$$6b - 10 = 6b - 10$$

$$-6b \quad -6b$$

$$-10 = 10$$

infinitely many solutions

Practice

1) $6r + 7 = 13 + 7r$

$$r = -6$$

2) $13 - 4x = 1 - x$

$$x = 4$$

3) $-7x - 3x + 2 = -8x - 8$

$$x = -\frac{5}{2}$$

4) $-8 - x = x - 4x$

$$x = 4$$

5) $-14 + 6b + 7 - 2b = 1 + 5b$

$$b = -8$$

6) $n + 2 = -14 - n$

$$n = -8$$

7) $n - 3n = 14 - 4n$

$$n = 7$$

8) $7a - 3 = 3 + 6a$

$$a = 6$$

9) $5 + 2x = 2x + 6$

 \emptyset

10) $-10 + x + 4 - 5 = 7x - 5$

$$x = 1$$

11) $-8n + 4(1 + 5n) = -6n - 14$

$$n = -1$$

12) $-6n - 20 = -2n + 4(1 - 3n)$

$$n = 3$$